



MAGIC GEOMETRY

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Abstract:

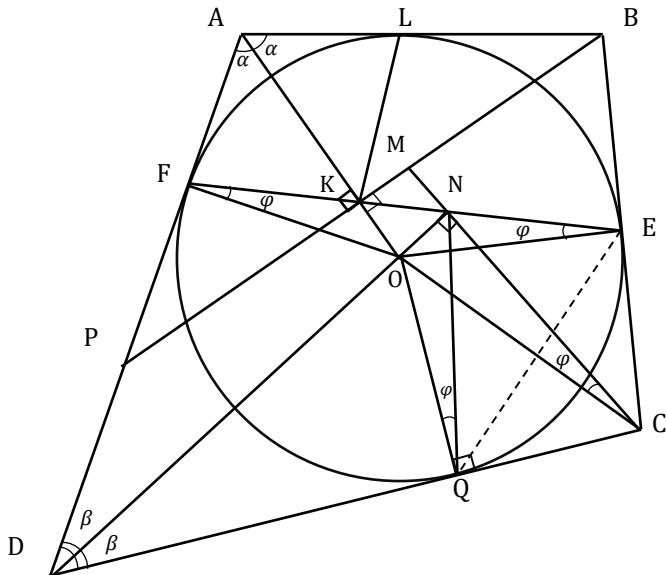
This article we will provide readers with interesting information about geometric issues and ways to solve them.

Keywords: circle, parallelogram, radius, angle.

Issue 1.

O centered circle ABCD is drawn internally into the rectangle. This circle is on the sides BC and AD at points E and F, respectively urinadi. $AO \cap EF = K$, $DO \cap EF = N$ and $BK \cap CN = M$: O, K, M, N points lie in a single circle.

Proof: let ABCD be the point L of attempt with AB of an inner drawn circle. $\Rightarrow KL$ cross-section $\Rightarrow FA = AL$ va $\angle FAK = \angle KAL = \alpha \Rightarrow \Delta AFK = \Delta ALK \Rightarrow FK = KL, \angle PKF = \angle LKB$ va $\Delta PFK = \Delta AKB \Rightarrow FP = LB \Rightarrow AP = AB \Rightarrow \angle APB = \angle PBA = 90^\circ - \alpha \Rightarrow AK \perp BK$. (*)



Let the point of attempt of the circle with DC be Q. \Rightarrow Host White, OF, OE and OCS $\Rightarrow OQ \perp OC$ $\angle FDO = \beta$ bo`lsin va $\angle OFK = \varphi$ bo`lsin $\Rightarrow \angle ODQ = \beta$, $\angle NEO = \varphi$ va $\angle DNF = 90^\circ - \beta - \varphi$. $\angle FOD = \angle DOQ \Rightarrow \angle FON = \angle QON$ va $FO = QO \Rightarrow \Delta FON = \Delta NOQ \Rightarrow \angle QON = \varphi$ $\angle FNO = 90^\circ - \beta - \varphi \Rightarrow \angle FON = 90^\circ + \beta \Rightarrow \angle NOE = 90^\circ - 2\varphi - \beta$, $\angle QON = \angle OEN \Rightarrow ONEQ - siklik \Rightarrow \angle NQE = 90^\circ - 2\varphi - \beta \Rightarrow \angle OQE = 90^\circ - \beta - \varphi$. $OQ \perp CQ$ va $OE \perp CE \Rightarrow OECQ - siklik \Rightarrow \angle OCE = \angle OCQ = 90^\circ - \varphi - \beta$ va $\angle DNF = 90^\circ - \varphi - \beta \Rightarrow ONEC - siklik \Rightarrow \angle OCN = \varphi \Rightarrow ONCQ - siklik \Rightarrow ON \perp CQ$. (*) according to $AK \perp BK \Rightarrow \angle OKM = \angle ONM = 90^\circ \Rightarrow OKMN - siklik \Rightarrow O, K, M, N$ nuqtas lie in a single circle.▲

Issue 2

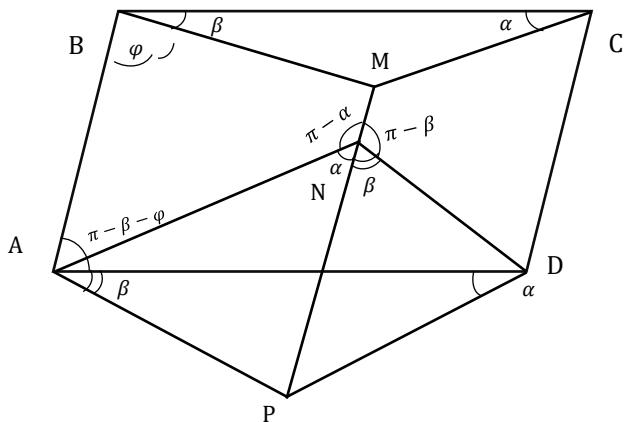
Inside the ABCD parallelogram, a point M is obtained, inside the ΔAMD , a point N is obtained. For these points, the condition $\angle MNA + \angle MCN = \angle MND + \angle MBC = 180^\circ$ is satisfied. Prove: $MN \parallel AB$

Proof: during MN we get such a point P, where ANDP is cyclic. $\Rightarrow \angle DNP = \angle DAP = \beta$ va $\angle ANP = \angle ADP = \alpha \Rightarrow \Delta ADP \sim \Delta BMC$ $AD = BC \Rightarrow \Delta ADP = \Delta BMC \Rightarrow BM = AP$ (1)

$\angle ABM = \varphi$ bo`lsin $\Rightarrow \angle PAD = \pi - \beta - \varphi \Rightarrow \angle BAP = \pi - \varphi \Rightarrow BM \parallel AP$ (2)



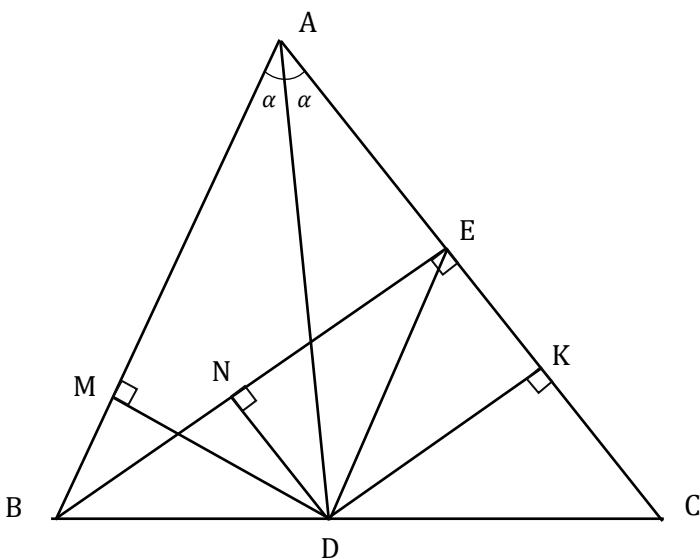
(1)Va (2) \Rightarrow BMPA- parallelogram $\Rightarrow AB \parallel MP \Rightarrow AB \parallel MP \Rightarrow \Delta$



Issue 3.

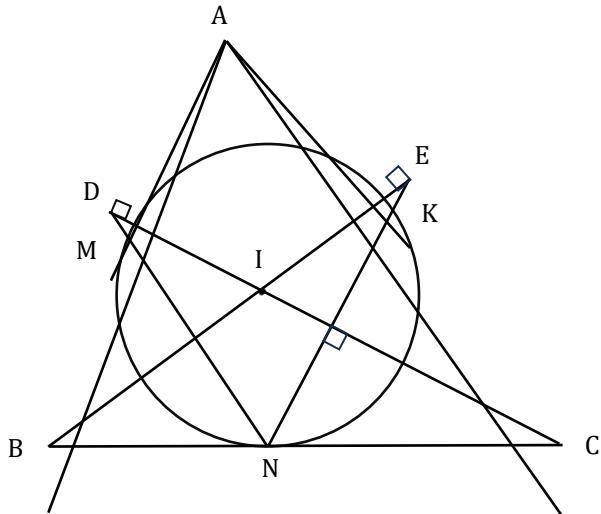
$\triangle ABC$ is a triangle with an acute angle. AD bissectira and BE held Heights. Prove: $\angle CED > 45^\circ$

Isbot: $M \in AB$, $K \in AC$, $N \in BE$ let it be here $DM \perp AB$, $DK \perp AC$, $DN \perp BE$ $\triangle ABC$ acute angle. \Rightarrow these points lie in suitable cuts. $DN \perp BE$ $BE \perp EK$, $DK \perp EK \Rightarrow DNEK$ right round $\Rightarrow NE = DK$ va $ND = EK$ AD- bisectira $\Rightarrow \triangle MAD = \triangle DAK \Rightarrow DK = DM$ $DM > DP > DN = EK \Rightarrow DK > EK$ ($MO \cap BN = P$) $\Rightarrow \angle DEK > \angle EDK \Rightarrow \angle DEK = \angle DEC > 45^\circ \Rightarrow \Delta$



Issue 4.

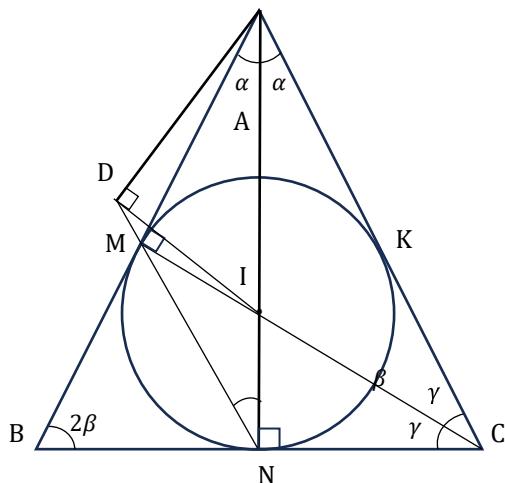
An inner drawn circle to ABC tries at points M, N and K, respectively, to sides AB, BC and CA. A straight line passed from point a parallel to NK intersects MN at Point D. A straight line transferred from point A to mn as a parallel lel intersects NK at point E. Prove: the de straight line Δ contains the midline of ABC.



Proof: Let the center of the circle drawn internally to $\triangle ABC$ be point I . $\Rightarrow CI \perp NK$

LEMMA; $\triangle ABC$ to inner drawn circle AB , BC va CA s respectively M , N , K let it urinate in points. (I – Circle Center). $MN \cap CI = K$ let. $\Rightarrow AK \perp CI$.

Proof: $\angle A=2\alpha$, $\angle B=2\beta$, $\angle C=2\gamma$ let. $MBNI$ - siklik $\Rightarrow \angle MNI=\beta$ va $\angle NCI=\gamma \Rightarrow \angle NKC=\alpha$ va $\angle MAI=\alpha \Rightarrow KMIA$ -siklik $\Rightarrow \angle AKI=90^\circ \Rightarrow AK \perp CI$ \Rightarrow Lemma proved. $\Rightarrow NK \parallel AD \Rightarrow D$, I , va C collinear. Similarly the points E , I , B are collinear.



LEMMA; bo'lisin let ω , drawn internally to $\triangle ABC$, be the center of the circle I . let the points of ω that are tried with AB , BC , CA be M , N , K . \Rightarrow The midline opposite CI , MN and BC intersects at one point.

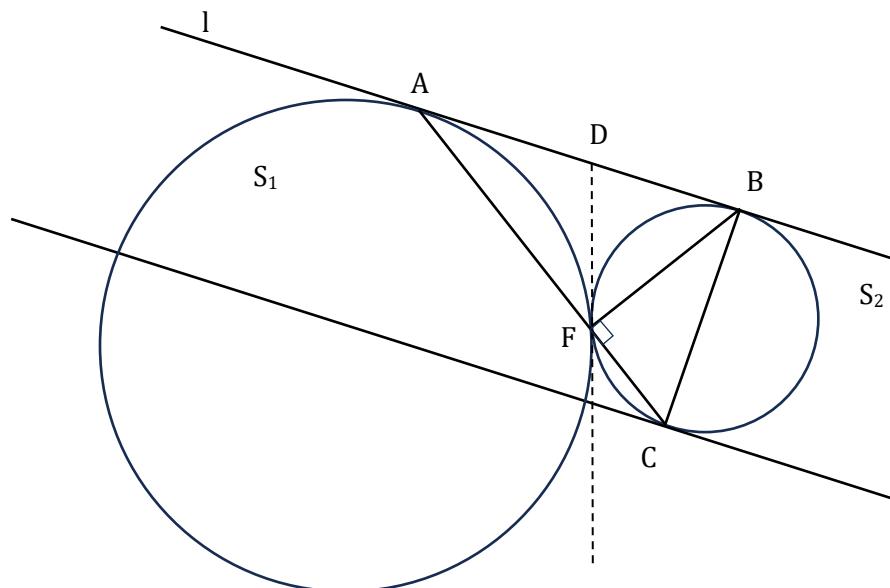
So a straight line transferred from point D to BC passes through the middle of the AB and AC s. Similarly a straight line transferred from point E to BC passes through the grooves of AB and AC s. $\Rightarrow D$ and points E lie on the midline of the Triangle. $\Rightarrow \blacktriangle$

Issue 5.

Circles S_1 and S_2 urinate externally at point F , A Straight Line l urinates at points A and B , respectively S_1 and S_2 . straight line parallel to l



Cuts to S_2 at Point C and S_1 at two points. Prove: points A, F and C collinear



Proof: the BC cross section passes through the center of S_1 . $\Rightarrow \angle BFC = 90^\circ$ from point urination. $\Rightarrow AD=DF$, $DF=DB \Rightarrow BF \perp AF \Rightarrow A, F, C$ the dots are collinear.

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